

3/6

Third year Communications



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اجب على الاسئلة الآتية

يرجى التأكد من وجود 7 أوراق بالكراسة مشتملة صفحة بيساء في نهاية الكراسة
السحرة عم كفاية المساحة المخصصة لإجابة أحد الاسئلة، اكمل الإجابة في المساحة المقابلة له أو في المساحة المخصصة نهاية الكراسة

Question #1 (Total 12 points)

Define and implement the class `sq_matrix` which represents a square matrix of doubles. The dimension of matrix is less than 100. The class supports the following operations: (4 points for proper class declaration)

- (2 points) `square_matrix(unsigned int dim)`: it sets the dimension of the matrix to `dim` and the elements are initialized to zeros. It must check that `dim` is less than 100.
- (3 points) `Add(const matrix &B)`: which adds matrix `B` to current matrix. The operation is only if the two matrices are of the same dimension.
- (3 points) `Copy(const matrix &B)`: which copies matrix `B` to current matrix overriding dimension stored values.



Question #2 (Total 20 points)

Using the standard singly linked-list storing items of ListElemType, add the following member functions:

- Split(ListElemType pivot, List &L2) which splits the list into two lists, all elements smaller than pivot remain in the current list and all elements greater than or equal to pivot move to list L2.
- Sort () : This function sorts the current list using the selection sort algorithm.

Write the definition of the class (4 points) and write the code of the above two member functions (8 points each)



Question#3 (Total 14 points)

a) (6 points) Write the code for binary search algorithm that searches a sorted array `a[]` of integers for the element equal to `key`. The array size is passed as parameter `n`.

b) (4 points)



c) (4 points)

3

when searching for 24.

Question #4 (Total 16 points)

a) (8 points) Write an external function `Boolean Identical(const Queue &Q1, const Queue &Q2)` that determines if the two queues are identical. Preconditions: Q1 and Q2 have been initialized. Postconditions: Queues are unchanged and function return value is true if the two queues are identical, false otherwise.

b) (8 points) Write an external function `int replace(Stack &S, Stack &T, int Value)` that uses member functions of the stack ADT to replace all occurrences of `Value` in `S` with the top element of `T`. The rest of the stack `S` remains unchanged.

Question#5 (Total 18 points)

Consider the implementation of the chained hash tables, with the standard operations of lookup, deleteKey, and insertKey. The entries in the table is kept in an array with maximum size MAX_TABLE_SIZE, however, the actual table size can be smaller than MAX_TABLE_SIZE and is kept in a private variable called tableSize that is passed as parameter to the constructor, i.e. the constructor of the Table class will look as follows:

Table::Table(int t_size). For simplicity you may disregard the usage of templates for this question.

i- (6 points) Write the code for the new constructor function which should assure that $t_size \leq \text{MAX_TABLE_SIZE}$. If t_size is equal to zero, the table size becomes MAX_TABLE_SIZE.

ii- (12 points) Write the code for the copy constructor function (Table &t1) that copies the contents of the current table is erased and the new table is created with the same size as the original table.



اجب على الأسئلة الآتية

يرجى التأكد من وجود ٦ أوراق بالكراسة مشتملة بصفحة بيضاء في نهاية الكراسة
في حالة عدم كفاية المساحة المخصصة لإجابة أحد الأسئلة، أكمل الإجابة في الصفحة المقابلة له أو في المساحة المخصصة نهاية الكراسة

Question #1 (Total 15 points)

Define and implement the class Polynomial which represents polynomial of the form $P(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x^1 + a_0$. The degree of the polynomial n is less than 100. The class supports the following operations: (4 points for proper class declaration)

(2 points) Polynomial (unsigned int deg): it sets the degree of the polynomial to deg and all the coefficients $\{a_i\}_{i=0}^{deg}$ are initialized to zeros. It must check that deg is less than 100.

(3 points) Polynomial (unsigned int deg, double a[]): it sets the degree of the polynomial to deg and all the coefficients $\{a_i\}_{i=0}^{deg}$ are initialized with the values in the array a[]. It must check that deg is less than 100.

(5 points) Polynomial* Add(const Polynomial &B): which adds polynomial B to the current polynomial and returns a pointer to the resulting polynomial. The degree of the resulting polynomial is the larger of the two polynomials' degrees.

Question #2 (Total 18 points)

Define a single-linked circular list (CircList) ADT supporting the standard's list operations of First, Next, Insert. In addition the list supports the operations void Merge(const CircList &clist) which merges clist with current list and the operation ReversePrint which prints the elements in the list in reverse order without using any additional structures. Write the definition of the class and the functions Insert, Merge, and ReversePrint.



Queue ADT (Total 12 points)

b) (6 points) Write an external function `int Replace(Queue &Q, QueueElemType item, QueueElemType newValue)` that uses member functions of the queue ADT to replace all occurrences of `item` with `newValue` leaving the rest of the queue unchanged. The function returns the number of queue entries that were replaced.

b) (6 points) Show how the following postfix expression is evaluated. What is the final result? $5\ 3\ * \ 8\ - \ 4\ + \ 3\ 2\ / \ - \ +$

Question 4 (Total 14 points)

The following is an algorithm known as InsertSort that sorts array a in ascending order.

```
void insertionSort(int a[], int n)
{
    int x; // item in the array
    int i, j;
    for (i=1; i < n; i++){
        x = a[i];
        j = i - 1;
        while (j >= 0 && a[j] > x){
            a[j+1] = a[j];
            j--;
        } // end while
        a[j+1] = x;
    } // end for
}
```

a) [8 points] Trace the execution of the algorithm on the array [5, 7, 13]

b) [6 points] Find the best and worst case time complexities (the big O) as function of n (array size).

Best case:

Worst case:

Question 1: True or False

a) [10 points] Classify the following statements as T or F, with brief explanation why.

- i) Binary search is an $O(n \log n)$ algorithm.
- ii) Binary search is always faster than sequential search.
- iii) When hashing is used increase size of hash table array always reduces the number of collisions.
- iv) If we use chaining in a hashing scheme we don't have to worry about collision resolution.
- v) For population size of 50, a table of size 101 with prime number 101 will always provide better collision performance if table size is 101.

b) [10 points] Consider the keys 6 47 87 9 126 153 566 620 735. Show how these values will be stored in a hash table:

- i) Using linear probing with a hash table of size 20.
- ii) Using chained hashing with a table of size 10.

Then fill the provided table indicating the number of comparisons for each given key.

Linear Probing

1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	

Chained Hashing

1	
2	
3	
4	
5	
6	
7	
8	
9	

#of comparisons

Key	Linear Probing	Chained Hashing
87		
566		
153		

أجب على الأسئلة الآتية

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المخصصة نهاية الكراسة

Q1 (20 points)

briefly what is meant by the following terms and their role in Object-Oriented Design and Programming:
Abstraction



Define an abstract class for the ComplexVector class. The ComplexVector class is a class of complex numbers. Each element of the vector is a complex number. The ComplexVector class supports the operation of adding two complex vectors. The class contains upto 100 complex numbers. The table below shows the definition of the ComplexVector class. You need to select the proper return types for all member functions. Don't include the Complex class ADT.

ComplexVector(int Size)	The class constructor that sets the size of the complex vector to Size and initialized all elements of the vector to (0+j0).
Elem(int i, const Complex &c)	Sets the value of element i of the vector to c. It should check that i is less than size of the vector.
Add(const ComplexVector &x)	Adds the vector x to the current object. The function should first assert that the two vectors have the same size, if so the addition is performed.
DotProduct(const ComplexVector &x)	Calculates the dot product of the vector x and the current object. The function should first assert that the two vectors have the same size, if so the addition is performed.

standard single-linked list ADT storing items of ListElemType. Write code for the following member

(6 points) Interchange: This function will consider each two adjacent nodes together and exchange the data in them. So, starting with the head as node 0, the contents of nodes 0 and 1 will be exchanged, nodes 2 and 3 will be exchanged and so on. If the list contains an odd number of nodes, the contents of the last node will not be exchanged with any other node.

(6 points) Reverse: This function will reverse all the nodes in the list in place without using any additional structures. The function should return the head of the reversed list. The list has N nodes.

(8 points) Destroy: This function will destroy the list by deleting all the nodes, destroying all previously stored items in the list.

(16 points)

Two stacks are implemented in one array of length 100 as shown. The tops of the stacks are pointed to $top1$ and $top2$ and grow toward each other. Write a procedure `int push (dataType v, int s)` that pushes the contents of v onto the stack indicated by s , where s is a value of 1 or 2. If the stack to which v is to be added is full, then push should return -1, if push succeeds it returns s . At initialization $top1 = 0$ and $top2 = 100$. Provide the condition for a full stack.



(points)

ing other el
ter the oper

On element of a queue,
value indicating

Cancelled & solved before

20 points

implementation of the chained hash tables with keys of type `KeyDataType` and associated data of type `DataType`, supporting the standard operations `lookup`, `deleteKey`, and `insert`. The entries in the table is kept in an array of maximum size `MAX_TABLE_SIZE`, however, the actual table size can be smaller than `MAX_TABLE_SIZE` and is stored in a private variable called `tableSize` that is passed as parameter to the constructor, i.e. the constructor of `Table` will look as follows: `Table::Table(int t_size)`. For simplicity you may ignore templates usage for this problem.

(10 points) Write the code for the new constructor function. Make sure that `t_size ≤ MAX_TABLE_SIZE`.

(10 points) Add a member function `merge(const Table &t1)` that merges the current table `t` with the table `t1`. Keep in mind that the number of slots in the table is determined by the value of `tableSize`.

When merging two tables, you need to look for key `lkey`. If and only if the node containing `lkey` is found in the current table, it is not moved to the new table (so if the node is found in the current table, it is not moved to the new table). If the node is not found in the current table, it is moved to the new table.

Final 2009 :

Question 1 :

*

```
const int maxsize = 100;
```

```
class sq_matrix {
```

```
private :
```

```
double
```

```
int
```

```
public :
```

```
sq
```

```
void Add
```

```
void Copy (const sq_matrix &B);
```

```
};
```

```
sq_matrix::sq_matrix (unsigned int dimn)
```

```
{ assert (dimn < maxsize);  
  dim = dimn;
```

```
for (int i=0; i<maxsize; i++)
```

```
for (int j=0; j<maxsize; j++)
```

```
A[i][j] = 0;
```

```
sq_matrix::Add
```

```
sq_matrix &B)
```

```
B.dim);
```

```
dim; i++)
```

```
dim; j++)
```

```
B.A[i][j];
```

```
::Copy
```

```
sq_matrix &B)
```

```
dim = B.dim;
```

```
for (int i=0; i<dim; i++)
```

```
for (int j=0; j<dim; j++)
```

```
A[i][j] = B.A[i][j];
```


Final 2009 :

Question 1 :

*

```
const int maxsize = 100;
```

```
class sq_matrix {
```

```
private :
```

```
double
```

```
int
```

```
public :
```

```
sq_
```

```
void Add
```

```
void Copy (const sq_matrix & B);
```

```
};
```

```
sq_matrix::sq_matrix (unsigned int dimn) {  
    assert (dimn < maxsize);  
    dim = dimn;  
}
```

```
for (int i=0; i<maxsize; i++)  
    for (int j=0; j<maxsize; j++)  
        A[i][j] = 0;
```

```
sq_matrix::Add (sq_matrix & B)
```

```
{  
    dim = B.dim;
```

```
    for (int i=0; i<dim; i++)
```

```
        for (int j=0; j<dim; j++)
```

```
            A[i][j] = B.A[i][j];
```

```
sq_matrix::Copy (sq_matrix & B)
```

```
{  
    dim = B.dim;
```

```
    for (int i=0; i<dim; i++)
```

```
        for (int j=0; j<dim; j++)
```

```
            A[i][j] = B.A[i][j];
```

Question 2 :

* class definition :

typedef int listElemType;

class list {

private:

struct node;

typedef node*

struct node

listElemType

link next;

link head; link cur;

public:

list();

bool first(listElemType elem);

bool next(listElemType elem);

void insert(listElemType elem);

void split(listElemType

pivot, list & L2);

void sort();

};

* void list::split
(listElemType elem,
list & L2)

{

link del;

link (head & L2

head->elem >= pivot)

link (head->elem);

del = head;

del->next;

del = del->next;

}

link head; link cur;

if (head->elem < pivot)

del = head->next->elem

>= pivot)

{ L2.insert(pred->next->elem);

del = pred->next;

pred->next = del->next;

delete del;

else

pred = pred->next;

{ }

void list::sort ()

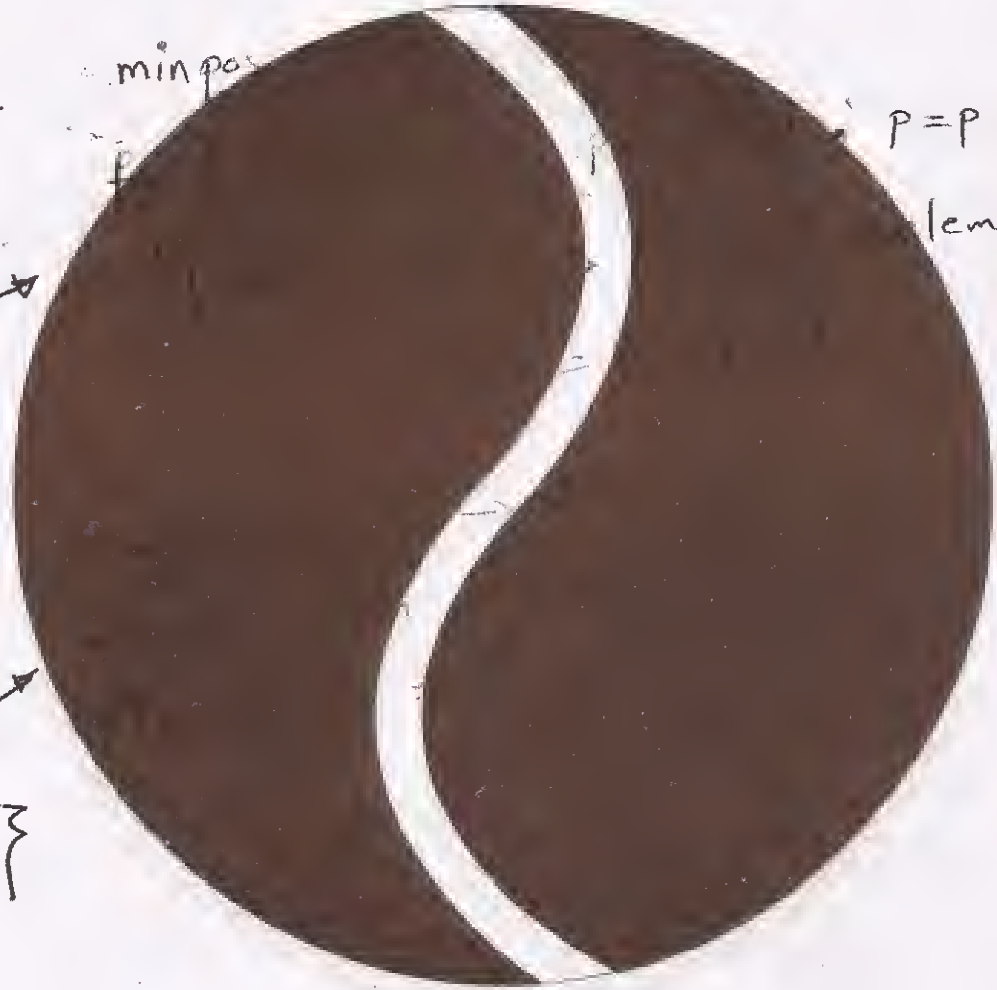
```
{
    link minpos, p; listElemType temp;
    for (link ptr=head; ptr && ptr->next; ptr=ptr->next)
```

of for
1
temp
list

```
{
    minpos = ptr;
    p = ptr->next;
    while (p != NULL)
    {
        if (p->data < minpos->data)
            minpos = p;
        p = p->next;
    }
    if (minpos != ptr)
    {
        swap(ptr->data, minpos->data);
    }
    ptr = ptr->next;
    }
}
```

2
ptr
for min

3
swap
in with
first elem



Question 3:

• a & b : see notes

• c) first step:

first = 0, last = 6

mid = $\frac{0+6}{2} = 3$

$$a[3] < \text{key}$$

17 24

$$\text{first} = \text{mid} + 1 = 4$$

Second step:

$$\bullet \text{ first} = 4, \text{ last} = 6, \text{ mid} = \frac{4+6}{2} = 5$$

$$\bullet a[5] < \text{key}$$

23

Third step:

$$\bullet \text{ first} = 6, \text{ last} = 6$$

$$\bullet a[6] > \text{key}$$

27

Fourth step:

Question 4:

[a]

bool identical (const Queue & Q1,
const Queue & Q2)

}

Queue Q3, Q4;

QueueElemType x, y; bool flag = true;


```

bool temp1 = Q1.isEmpty();
bool temp2 = Q2.isEmpty();
while (!temp1 && !temp2)

```

```

{
    x = Q1.dequeue(); Q3.enqueue(x);
    y = Q2.dequeue(); Q4.enqueue(y);

```

```

}

```

```

while (

```

```

    Q1.enqueue

```

```

while (!Q

```

```

    Q2.enqueue (Q

```

```

if ((!temp1 && !temp2) || temp1 || temp2)

```

```

    flag = false;

```

```

return flag;

```

```

}

```

⑥ Solved before.

Question 5:

i - solved before.

ii -

```
void Table::Copy (Const Table &t)
```

```
{
```

```
    link del
```

```
    for (int i = 0; i < t.GetSize(); i++)
```

```
    {
```

```
        int data;
```

```
        P->
```

```
        tableSize = t.GetSize();
```

```
        for (int i = 0; i < t.GetSize(); i++)
```

```
        {
```

```
            insert
```

```
            , P->data);
```

```
}
```

Final 2010

Question 1:

```
const int N=100;
```

```
class Polynomial {
```

```
private:
```

```
double Arr[N];
```

```
int n;
```

```
public:
```

```
Polynomial()
```

```
Polynomial(int deg)
```

```
Polynomial(Polynomial &A)
```

```
Polynomial(Polynomial &A,
```

```
};
```

```
Polynomial::Polynomial  
(unsigned int deg)
```

```
{  
    assert(deg < N);
```

```
    n = deg;
```

```
    for (int i=0; i<=n; i++)
```

```
        Arr[i] = 0;
```

```
Polynomial::Polynomial
```

```
(unsigned int deg,  
double arr[])
```

```
{  
    assert(deg < N);
```

```
    for (int i=0; i<=n; i++)
```

```
        Arr[i] = arr[i];
```

```
Polynomial::Add
```

```
(Polynomial &B)
```

```
{
```

```
    int nmax = n, nmin = B.n;
```

```
    Polynomial* P = new Polynomial  
(nmax);
```

```
    for (int i=0; i<=nmin; i++)  
        P->Arr[i] = Arr[i] + B.Arr[i];
```

```
    if (n == nmax)  
        for (int i=nmin+1; i<=n; i++)  
            P->Arr[i] = Arr[i];
```

else

for ($i = \text{nmin} + 1; i \leq B.n; i++$)

$p \rightarrow \text{Arr}[i] = B.\text{Arr}[i];$

return p ;

}

Another solution (for polynomial $\neq B$)

Polynomial

{

Polynomial p ;

if ($n > B.n$)

{ $p = \text{new polynomial}(n);$

for ($i = 0; i \leq n; i++$)

if ($i \leq B.n$)

$p \rightarrow \text{Arr}[i] = B.\text{Arr}[i];$

else $p \rightarrow \text{Arr}[i] = 0;$

} else { $p = \text{new polynomial}(B.n);$

for ($i = 0; i \leq B.n; i++$)

if ($i \leq n$)

$p \rightarrow \text{Arr}[i] = \text{Arr}[i] + B.\text{Arr}[i];$

else

$p \rightarrow \text{Arr}[i] = B.\text{Arr}[i];$

}

return p ;

}

Question 2:

→ Definition:

```
typedef int listElementType;  
class CircleList {
```

private:

struct

listElement {

public:

bool

bool

bool

or
void

void

void

};

Merge (const CircleList &clList);

ReversePrint ();

→ Functions :

bool CirList :: insert (Const listElemType &e)

{

link addedNode = new node;

if (!addedNode) return false;

if (!head)

{

addedNode->elem = e;

addedNode->next = head;

head = addedNode;

return true;

}

else

{

addedNode->next = head->next;

head->next->elem = e;

addedNode->elem = e;

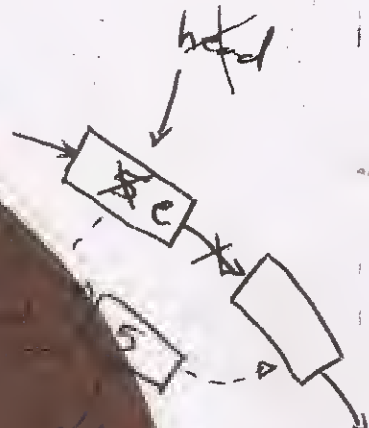
head->elem = e;

head = addedNode;

return true;

}

}



• void CirList::Merge (const CirList &clist)

```
{
    if (clist.head == 0) return;
    for (link p = clist.head; p->next != clist.head;
        p = p->next)
```

```
    if (!insert(p->elem))
```

```
    // Support
    // nodes
```

or multiple

• void

```
{
    if (!head)
        link p;
    for (p = head; p->next != head; p = p->next)
        N++;
```

```
listElemType * A = new listElemType [N];
```

```
for (p = head; p->next != head; p = p->next)
```

```
{ A[i] = p->elem; i++; }
```

```
A[i] = p->elem;
```

```
for (i = N-1; i >= 0; i--)
```

```
    cout << A[i];
```

```
delete [] A;
```

```
}
```

Another Solution

```
void CircList::Reverse()
```

```
{ if (!head) return;
```

```
    Stack < int> s;
```

```
    for (link p = head; p != NULL; p = p->next)
```

```
        s.push(p->data);
```

```
    s.push(p->data);
```

```
    while (!s.isEmpty())
```

```
        cout << s.pop();
```

```
}
```


Third Solution :

void CirList::ReversePrint()

{ if (!head) return;

int i, j, N = 1; link p;

for (p = head; p != p->next)

for (i = 1;

{

p = head;

cout << p->data << " ";

}

}

Question 3:

9

int Replace (Queue & Q, QueueElementType item,
QueueElementType newValue)

{ int N=0; QueueElementType X;

Queue

while (!Q.IsEmpty())

{ X = Q.Dequeue();

if (X == item)

{ Q.Enqueue(newValue); N++; }

else

Q.Enqueue(X);

}

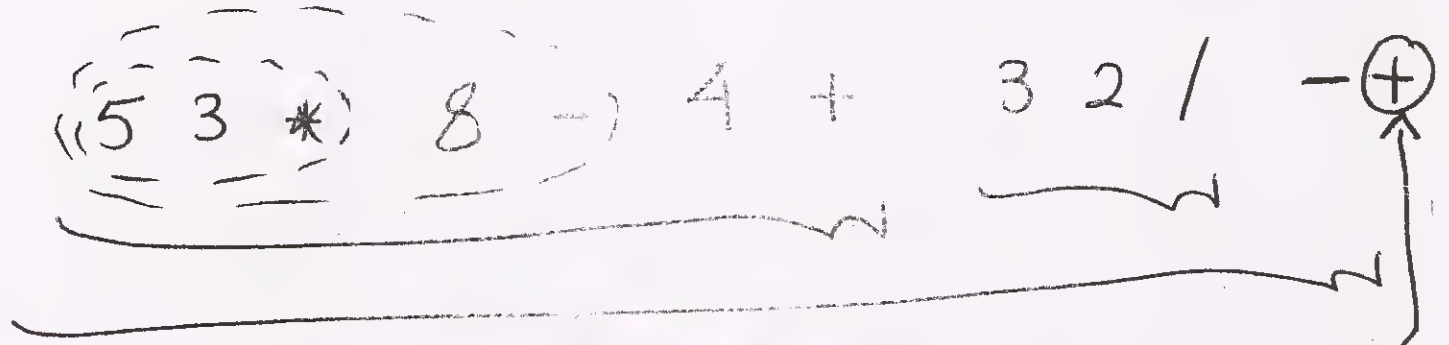
while (!Q.IsEmpty())

Q.Enqueue(Q.Dequeue());

return N;

}

b) RPN using stacks.



Unused operator

- Synt
- ext
- th



Question 5:

a

i- T, proof of binary search

"Cancelled"

ii- F, only in

"Cancelled"

iii- T

iv- T

v- T

b

i-

Linear

Probing

False

size = 20

key

key

key

key

Comp.

66
47
87
90
126
140
145
153
177

6
7
7
10
6
0
5
13
17

6
7
8
10
9
0
5
13
17

1
1
2
1
4
1
1
1
1
1

30

285	5	11	7
393	13	14	2
395	15	15	1
467	7	12	6
566	6	16	11
620	0	1	2
735	15		4

mod 20

→ Pr

→ Fin

2	
3	
4	
5	145
6	66
7	47
8	87
9	126
10	90
11	285
12	467
13	153
14	393
15	395

6
7
735
—

no. of Comp.

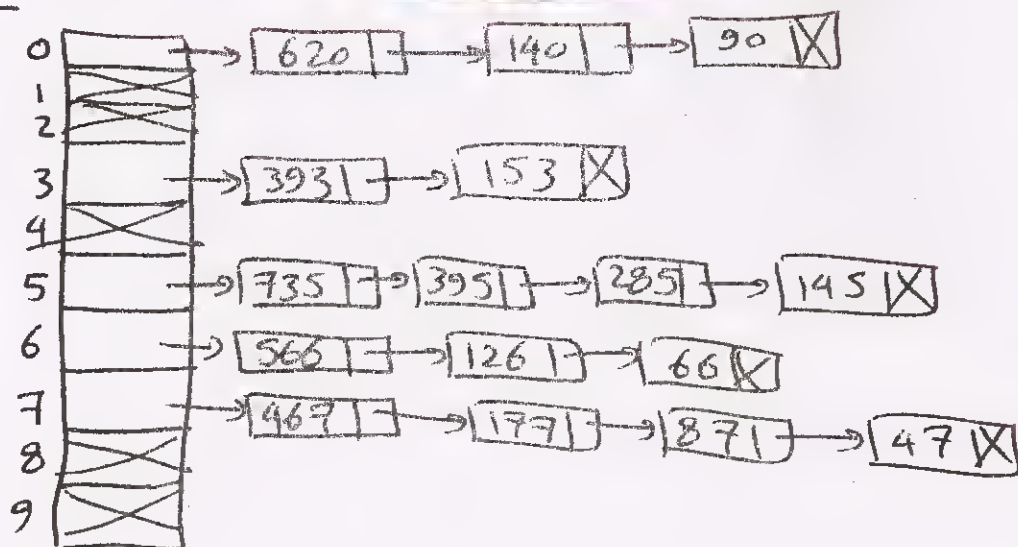
87	2
566	11
153	1

ii- Chained Table :

Table size = 10

key	hash o/p	no. of Comp
66	6	3
47	7	4
87	7	3
90	0	3
126	6	2
140		2
145		4
153		
177	7	
285	5	
393	3	
395	5	
467	7	
566	6	
620	0	
735	5	

Table :



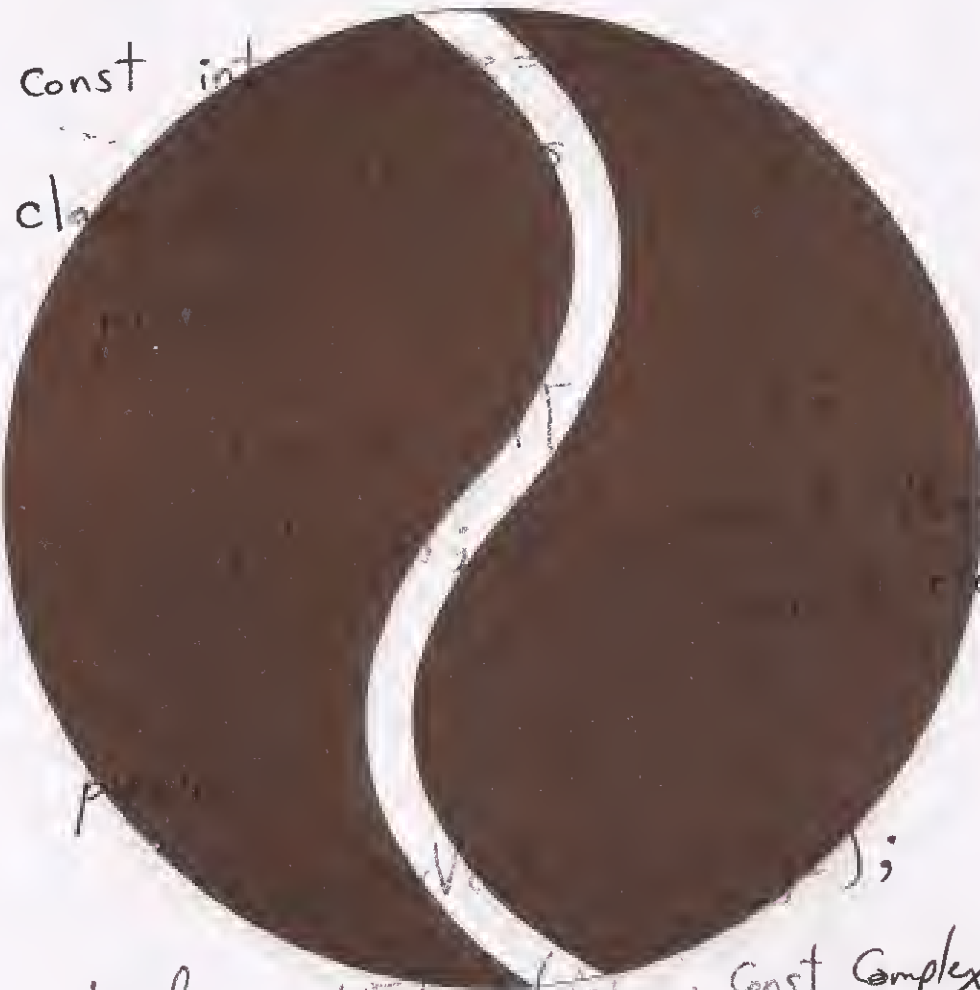
Final 2011

Q1. b.

```
#include "Complex.h"
```

```
const int
```

```
class
```



elements

```
private:
```

```
bool SetElem (int, const Complex &c);
```

```
void Add (const ComplexVector &x);
```

```
Complex DotProduct (const ComplexVector &x);
```

```
};
```

ComplexVector :: ComplexVector (int size)

```
{  
    assert (size <= maxsize);  
    N = size;  
    for (int i=0; i < maxsize; i++)
```

```
{  
        A[i].setreal(0);
```

```
        A[i].setimag(0);
```

```
}
```

```
}
```

bool

ComplexVector ::

+

Complex

= c)

```
{
```

```
if (i >= N)
```

```
return false;
```

```
A[i].setreal (c.getreal());
```

```
A[i].setimag (c.getimag());
```

```
return true;
```

```
}
```


void ComplexVector::Add (const ComplexVector &x)

{

assert (N == x.N);

for (int i=0; i<N; i++)

{

A[i].real() + x.A[i].real();

+ x.A[i].imag();

}

⇒ You can't deal with complex numbers directly.

So, the loop will be :

for (int i=0; i<N; i++)

A[i].Add (x.A[i]);

Complex ComplexVector::DotProduct (const ComplexVector &x)

{

assert (N == x.N);

Complex sum, temp;

sum.Setreal(0); sum.Setimag(0);

for (n = 0; n < N; n++)

{ temp.Setreal(0); temp.Setimag(0);

temp.Setreal(A[n].real * x[n].real - A[n].imag * x[n].imag);

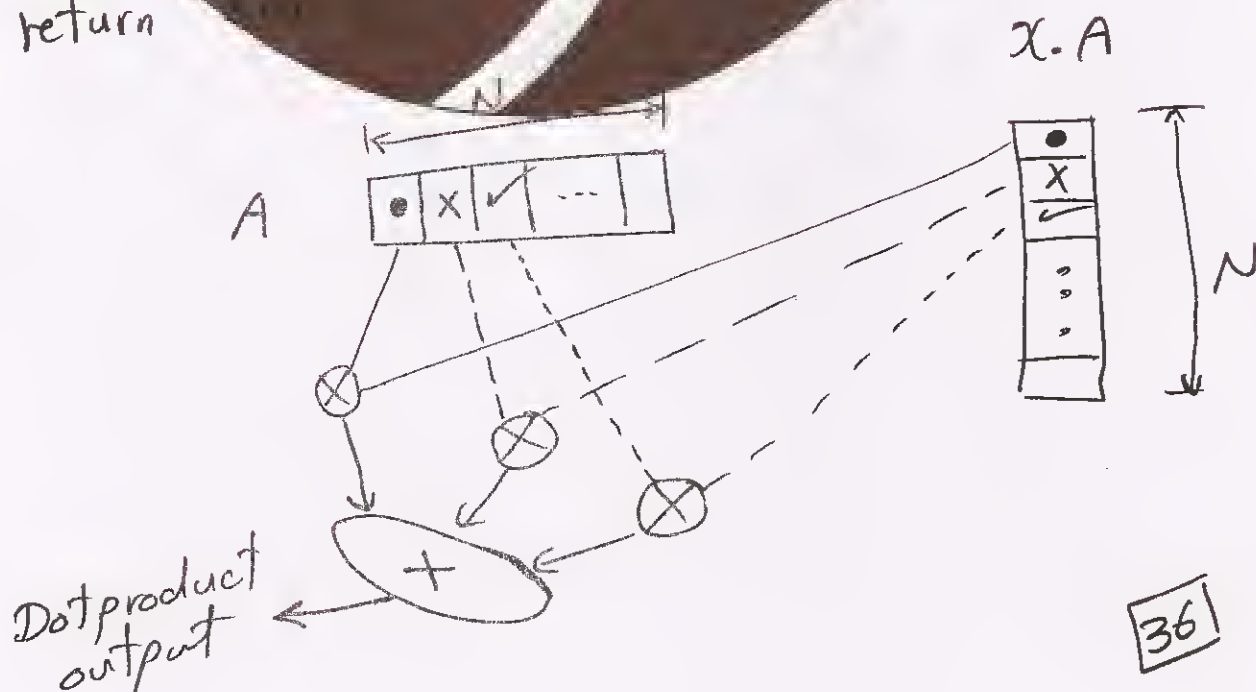
temp.Setimag(A[n].real * x[n].imag + A[n].imag * x[n].real);

sum.Add(temp);

}

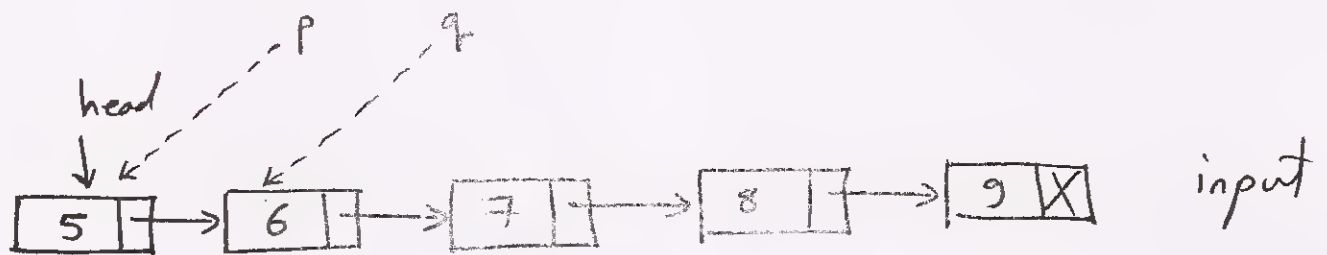
return sum;

}



Q2.

9



Void

{

Link

link

while (q)

```
{ temp = p->elem;
  p->elem = q->elem;
  q->elem = temp;
```

```
  p = q->next;
```

```
  if (p != p->next) q = p->next;
```

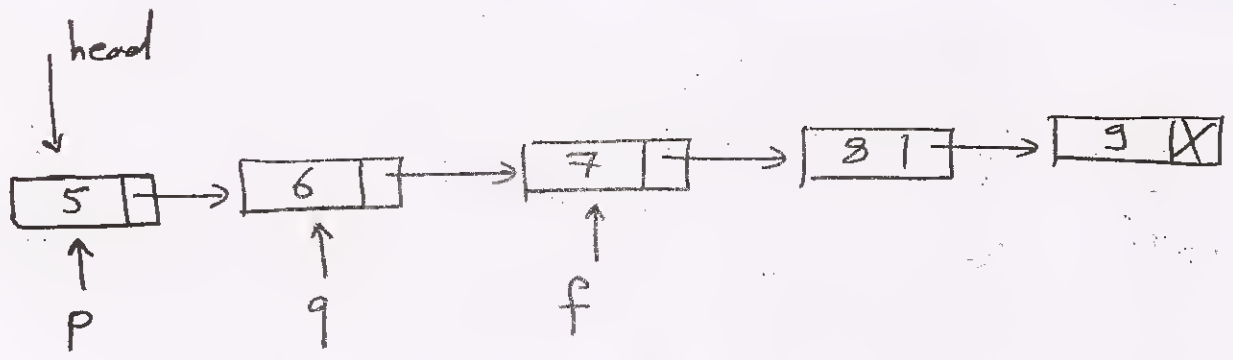
```
  else q = 0; }
```

return;

next;

}

b



void list::Reverse()

```

{
    if (head == null || head->next == 0) return;
    link f;
    link p = head;
    if (p->next)
    {
        f = p->next;
        p->next = 0;
        f->next = p;
    }
    while (f)
    {
        p = f;
        f = f->next;
        p->next = f;
    }
    head = p;
}

```


c

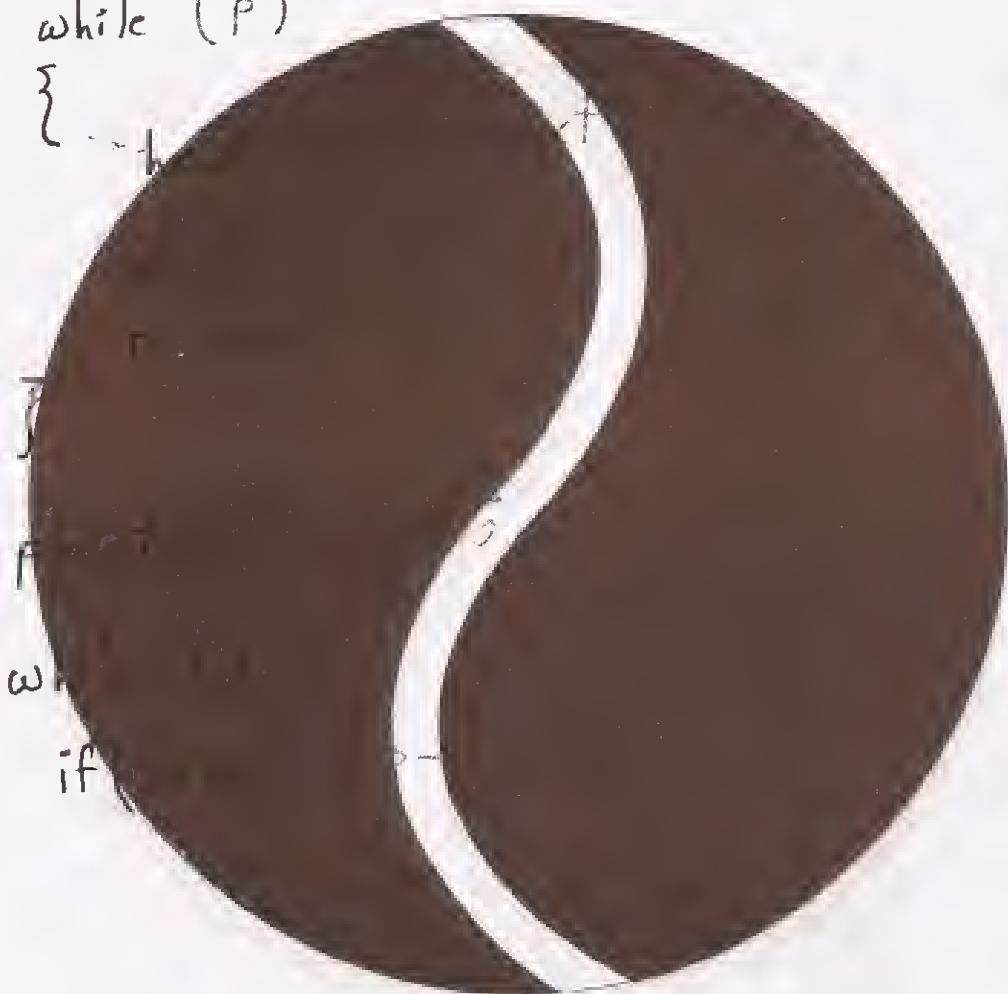
void list == Copy (const list & otherlist)

{

link p = head;

while (p)

{



if (p->next == NULL)

while (p)

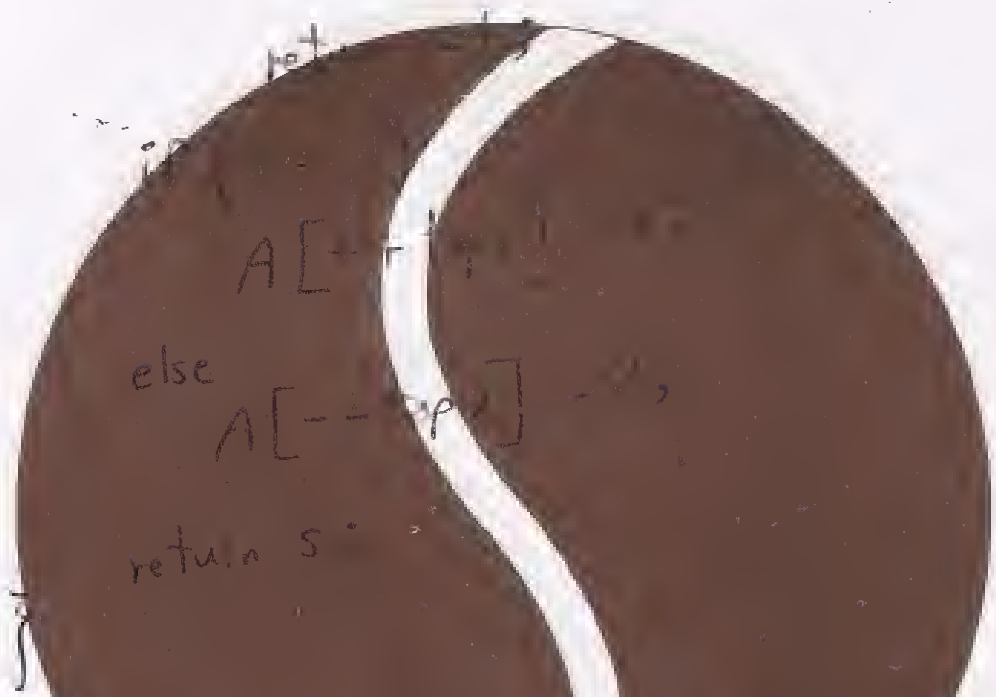
if

}

Q3.

a

```
int push (stackDataType v, int s)
{
    if (top2 == top1 + 1)
```



```
    A[top1] = v;
    top1++;
    return s;
}
```

b

```
bool isEmpty (Queue q, int n)
{
    Queue q;
    while (n >= 0 && !q.isEmpty())
    {
        x = q.dequeue();
        if (n != 0) T.enqueue(x);
        n--;
    }
    while (!T.isEmpty()) q.enqueue(T.dequeue());
    return (n == -1);
}
```

A General Test

Question 1:

Define an abstract data type, the class `ComplexMatrix`, that represents a square matrix of Complex numbers. Each element of the matrix is an object of the `Complex` ADT. The `Complex` ADT supports the operation `Add`, `Multiply`, and the `Set/Get` functions. The `ComplexMatrix` class contains upto 100 complex numbers per dimension and supports the member functions shown in the table below. Write the definition of the `ComplexMatrix` class and implement its member functions. You need to select the proper return type and argument. You don't need to write the `Complex` class ADT.

i) <code>ComplexMatrix(int dimn)</code>	to create a matrix of the matrix dimension should be <code>dimn</code> .
ii) <code>SetElement(int i, int j, Complex c)</code>	to set the element at (i,j) to c.
iii) <code>Multiply(ComplexMatrix m2)</code>	to multiply the matrix with m2. You should return the first element of the result matrix.

Question 2:

- The following is a recursive function to find the sum of the first n natural numbers. Write the base case and the recursive case.
- Write a recursive function to find the sum of the first n natural numbers. The function should return the sum of the first n natural numbers. The function should be named `sum`.

Question 3:

- The following is a recursive function to find the sum of the first n natural numbers. Write the base case and the recursive case. The function is called `quick` and it is called quick sort. The function should return the sum of the first elements in the array.

<pre>int partitioning (int a[], int first, int last) { int pos=first; for (int i=first+1; i<=last; i++) if (a[i]>a[first]) { pos++; swap(a,i,pos); } // end of loop swap(a,first,pos); return pos; } // end of partitioning</pre>	<pre>int temp=a[pos1]; a[pos1]=a[pos2];a[pos2]=temp; void sort (int a[],int first,int last) { if (first>=last) return; int pivot=partitioning(a,first,last); sort(a,pivot+1,last); sort(a,first,pivot-1); }</pre>
---	---

- a) Trace the above code for the following array 12 5 20 -3 9
- b) What is the number of comparisons in the worst case of this algorithm?
- ii. Write a class BinarySearch to search for certain target in an array of strings recursively.

Question 4:

- i. Write a function deloccurrence (stack & s, stackelementtype v) to delete all occurrence of the element v from the stack s
- ii. Write a function printprime, to print all prime numbers stored in a given Queue Q.
- iii. Write the definition of the standard circular queue class using linked lists and implement the enqueue function.

Question 5:

- i. Write the code for the following function: InsertNode (Node* Current, and UpdateCurrent to the Node* class. The function will perform two tasks respectively, i, add a node at the front of the linked list, and ii, by the current pointer, and update the data of the current node by the value.
- ii. Using the linked list class defined above. Define and implement a class that performs insert, lookup, and delete-key functions. The linked list is represented by an array of nodes.

Test solution

Question 1:

```
#include "complex.h"
const int MAXSIZE = 100;
Class ComplexMatrix {
public:
    ComplexMatrix(unsigned int dimn):
        void SetElem(int i, int j, const Complex &c):
        void Multiply(const ComplexMatrix &A, ComplexMatrix &B):
private:
    //the array for storing elements
    Complex Elements[MAXSIZE][MAXSIZE];
    int dim; //the dimension of the matrix
}

ComplexMatrix::ComplexMatrix(unsigned int dimn):
{
    int i, j;
    assert(dimn < MAXSIZE);
    dim = dimn;
    for(i=0; i < dim; i++)
        for(j=0; j < dim; j++)
        {
            Elements[i][j].SetReal(0);
            Elements[i][j].SetImag(0);
        }
}

void ComplexMatrix::SetElem(int i, int j, const Complex &c)
{
    assert(i < dim && j < dim);
    Elements[i][j].SetReal(c.GetReal());
    Elements[i][j].SetImag(c.GetImag());
}

ComplexMatrix ComplexMatrix::Multiply(const ComplexMatrix &B)
{
    assert(dim == B.dim);
    int i, j, k;
    ComplexMatrix Result(dim);
    Complex temp;
    for(i=0; i < dim; i++)
        for(j=0; j < dim; j++)
            for(k=0; k < dim; k++)
                Result.Elements[j][k] = Elements[j][i] * B.Elements[i][k];
    return Result;
}

ComplexMatrix::operator ComplexMatrix &() const
{
    return *this;
}
```


Question 5:

i- The code of the list will be:

```
#include<assert.h>
template <class ListElementType>
class List
{
public:
    List();
    void insert(const ListElementType & elem);
    bool first(ListElementType & elem);
    bool next(ListElementType & elem);
    void UpdateCurrent(const ListElementType & elem);
    void InsertAtBeginning(const ListElementType & elem);
    void deleteCurrent();
private:
    struct Node;
    typedef Node *Link;
    struct Node
    {
        ListElementType elem;
        Link next;
    };
    Link head;
    Link tail;
    Link current;
};

template <class ListElementType>
List<ListElementType>::List()
{
    head = 0;
    tail = 0;
    current = 0;
}

/////first(), next(), and insert() We use template <class
ListElementType> ] before
each function and the class name used is [ List<ListElementType> ] like:
template <class ListElementType>
void List<ListElementType>::insert(const ListElementType & elem)
//// member functions that we add:
template <class ListElementType>
void List<ListElementType>::UpdateCurrent(const ListElementType & e)
{
    assert(current);
    current->elem=e;
```

```

}
template <class ListElementType>
void List<ListElementType>::InsertAtBeginning(const ListElementType & e)
{
    Link addedNode=new Node;
    addedNode->next=head;
    addedNode->elem=e;
    head=addedNode;
}
template <class ListElementType>
void List<ListElementType>::Delete()
{
    assert(current);
    if(head==0)return;
    Link del; // if current is head
    if(head==current)
    {
        del=current;
        head=current->next;
        delete del;
        return;
    }
    // current is not head
    for(Link p=head; p->next!=current; p=p->next)
    {
        del=current;
        p->next=current->next;
        delete del;
    }
}

```

ii- The code

```

#include "list.h" //not needed in this file
const int MAX_TABLE = 100;
template < class tableKeyType, class tableDataType >
class Table
{
public:
    // Table(); we don't need a constructor, since the constructor of list class will cause each
    // head, tail and
    // current to be=0
    void insert(const tableKeyType & key, const tableDataType & data);
    bool lookup(const tableKeyType & key, tableDataType & data);
    void deleteKey(const tableKeyType & key);
    void dump();
private:

```

```

struct Slot
{
    tableKeyType key;
    tableDataType data;
};
List<Slot> T[MAX_TABLE]; // array of linked lists
int hash(const tableKeyType & key);
};
template <class tableKeyType, class tableDataType>
int Table<tableKeyType,tableDataType>::hash(const tableKeyType & key)
{
    return key % MAX_TABLE;
}
template <class tableKeyType, class tableDataType>
void Table<tableKeyType,tableDataType>::insert(const tableKeyType & key, const
tableDataType & data)
{
    int pos(hash(key));
    Slot s,s1;
    s1.key=key;s1.data=data;
    bool f=T[pos].first(s);
    if(f==false)T[pos].insert(s1); //if slot is empty
    else
    {
        while(f)
        { // if the key exists update slot
            if(s.key==key){T[pos].Update(s1);
            f=T[pos].next(s);
            }
            // if key doesn't exist, insert slot at beginning
            T[pos].InsertAtBeginning(s1);
        }
    }
}

```

```

template <class tableKeyType, class tableDataType>
bool Table<tableKeyType,tableDataType>::lookUp(const tableKeyType & key,
tableDataType & data)
{
    int pos(hash(key));
    Slot s; bool b;
    b=T[pos].first(s);
    while(b)
    {
        if(s.key==key)
        {data=s.data;return true;}
    }
}

```

```
b=T[pos].next(s);
```

```
}
```

```
return false;
```

```
}
```

In the previous function, we hash the key, traverse the list comparing the keys.

Remember that s is passed

by reference to first () and next() so after the call they contain an element (a slot) from the list.

```
template < class tableKeyType, class tableDataType >
```

```
void Table < tableKeyType, tableDataType >::delete (tableKeyType & key)
```

```
{
```

```
int pos(hash(key));
```

```
Slot s; bool b;
```

```
b=T[pos].first(s);
```

```
while(b)
```

```
{
```

```
if(s.key==key)
```

```
{T[pos].delete(s);
```

```
b=T[pos].next(s);
```

```
}
```

```
}
```

```
// delete the element
```

```
delete the element
```

```
which 'key' is
```

```
template
```

```
void Table
```

```
{
```

```
Slot s; bool b;
```

```
for (int i=0; i<T.size(); i++)
```

```
{
```

```
cout << i << '\t';
```

```
b=T[i].first(s);
```

```
while(b)
```

```
{
```

```
cout<<s.key<<'\t';
```

```
b=T[i].next(s);
```

```
}
```

```
cout << '\n';
```

```
}
```

```
cout << '\n';
```

```
}
```

Question 2:a

```
void list::sort()
```

```
{
```

```
if(head == 0 || head->next == 0)
```

```
return;
```

```
link t = head;
```

```
while (t->next != 0)
```

```
t = t->next;
```

```
link p2 = t;
```

```
while (t->prev != 0)
```

```
{
```

```
while (p1->next != t)
```

```
{ if (p1->data > t->data)
```

```
{ temp = p1->data;
```

```
p1->data = t->data;
```

```
t->data = temp;
```

```
}
```

```
p2 = p1;
```

```
p1 = p1->prev;
```

```
}
```

```
t = t->prev; p2 = t;
```

```
if (p2->prev) p1 = p2->prev;
```

```
}
```

```
}
```

listElement pc
temp;

